

Trigonometry (For right triangle with sides Adjacent, Opposite, and Hypoteneuse):

$$\begin{aligned} \sin(\theta) &= O/H & \cos(\theta) &= A/H & \tan(\theta) &= O/A & H^2 &= O^2 + A^2 & A_{\text{circle}} &= \pi r^2 & \text{Circumference} &= 2\pi r \\ \sin(30^\circ) &= \cos(60^\circ) = 1/2 & \sin(60^\circ) &= \cos(30^\circ) = \sqrt{3}/2 \sim 0.866 & \sin(45^\circ) &= \cos(45^\circ) = \sqrt{2}/2 \sim 0.707 \\ \sin(0^\circ) &= \cos(90^\circ) = 0 & \sin(90^\circ) &= \cos(0^\circ) = 1 \end{aligned}$$

Moment of Inertia

$$\begin{aligned} \text{Point mass or thin-walled wheel or hoop: } & I = mr^2 & \text{Solid cylinder or disk: } & I = \frac{1}{2} mr^2 \\ \text{Thin rod pivoting around end: } & I = 1/3 mr^2 & \text{Solid sphere: } & I = 2/5 mr^2 \end{aligned}$$

Kinematics:

$$\langle \vec{v} \rangle = \frac{\Delta \vec{r}}{\Delta t} \quad \langle \vec{a} \rangle = \frac{\Delta \vec{v}}{\Delta t} \quad \vec{r} = \vec{r}_0 + \vec{v}_0 t + \frac{1}{2} \vec{a} t^2 \quad v^2 = v_0^2 + 2\vec{a} \cdot \Delta \vec{r}$$

Newton's Laws:

$$\sum \vec{F} = m\vec{a} \quad \vec{F}_{AB} = -\vec{F}_{BA}$$

Forces:

$$\begin{aligned} F_G &= mg \text{ (@ surface)} & f_s^{MAX} &= \mu_s F_N & f_k &= \mu_k F_N \\ F_C &= ma_c = \frac{mv^2}{r} & F_{\text{spring}} &= -kx & F_{\text{Buoyant}} &= m_{\text{displaced}} g \end{aligned}$$

Work & Energy:

$$\begin{aligned} KE_{\text{trans}} &= \frac{1}{2} mv^2 & \Delta KE &= W_{\text{net}} & PE_G &= mgh & PE_{\text{spring}} &= \frac{1}{2} kx^2 \\ E &= KE + PE & \Delta E &= W_{\text{nc}} & W &= \vec{F} \cdot \Delta \vec{r} = |\vec{F}| |\Delta \vec{r}| \cos \theta_{Fdr} \end{aligned}$$

Impulse & Momentum:

$$\begin{aligned} \vec{J} &= \vec{F} \Delta t & \vec{p} &= m\vec{v} & \sum \vec{J} &= \Delta \vec{p} & \sum \vec{p}_f &= \sum \vec{p}_i \text{ (if } F_{\text{ext}}=0) \\ \vec{v}_{cm} &= \frac{\sum m_i \vec{v}_i}{\sum m_i} = \sum \vec{p} / M \end{aligned}$$

Rotational Motion:

$$\begin{aligned} \theta &= s/r & \langle \omega \rangle &= \frac{\langle v_t \rangle}{r} = \frac{\Delta \theta}{\Delta t} & \langle \alpha \rangle &= \frac{\langle a_t \rangle}{r} = \frac{\Delta \omega}{\Delta t} & a_c &= v^2/r \\ \theta &= \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2 & \omega^2 &= \omega_0^2 + 2\alpha \Delta \theta \\ \tau &= rF \sin \theta_{rF} = F * \text{lever arm} & \sum \tau &= I\alpha & L &= I\omega = mvr \text{ (point mass)} \\ W_{\text{rot}} &= \tau \Delta \theta & KE_{\text{rot}} &= \frac{1}{2} I\omega^2 & r_{CM} &= \frac{\sum m_i r_i}{\sum m_i} \end{aligned}$$

Harmonic Motion:

$$\begin{aligned} \omega_h &= 2\pi f_h = \frac{2\pi}{T} = \sqrt{\frac{k}{m}} & x_{\text{max}} &= A & v_{\text{max}} &= A\omega_h & a_{\text{max}} &= A\omega_h^2 \\ \omega_{\text{pendulum}} &= \sqrt{\frac{mgr_{CM}}{I}} = \sqrt{\frac{g}{L}} \text{ for simple pendulum of length } L \end{aligned}$$

Fluids:

$$\rho = \text{mass/Volume}$$

$$\rho_1 A_1 v_1 = \rho_2 A_2 v_2$$

$$P = F/A$$

$$A_1 v_1 = A_2 v_2 \text{ (if } \rho_1 = \rho_2 \text{)}$$

$$P_2 = P_1 + \rho g d$$

$$F_B = W_{\text{fluid_displaced}}$$

Heat:

$$T_C = \frac{5}{9}(T_F - 32)$$

$$T_K = T_C + 273.15$$

$$\frac{\Delta L}{L} = \alpha \Delta T$$

$$\frac{\Delta V}{V} = 3\alpha \Delta T = \beta \Delta T$$

$$Q_{\text{specific}} = mc\Delta T$$

$$Q_{\text{latent}} = mL$$

$$\frac{Q_{\text{conduction}}}{t} = \frac{kA \Delta T}{L}$$

$$\frac{Q_{\text{radiation}}}{t} = e\sigma AT^4$$

Ideal Gas:

$$n = \frac{N}{N_A} = \frac{m}{M_{\text{molar}}}$$

$$PV = nRT = NkT$$

$$\langle KE \rangle = \frac{3}{2}kT$$

$$U_{\text{monatomic}} = \frac{3}{2}NkT = \frac{3}{2}nRT$$

Thermodynamics:

$$\Delta U = Q - W$$

$$W = P\Delta V = nR\Delta T \text{ (isobaric, const. } P) \quad W = nRT \ln\left(\frac{V_f}{V_i}\right) \text{ (isothermal, const. } T)$$

$$W = -\frac{3}{2}nR(T_f - T_i) \text{ (adiabatic, monatomic)}$$

$$P_1 V_1^\gamma = P_2 V_2^\gamma \text{ (adiabatic)}$$

$$Q = Cn\Delta T \quad C_{P_{\text{monatomic}}} = \frac{5}{2}R \quad C_{V_{\text{monatomic}}} = \frac{3}{2}R$$

$$\gamma = C_P/C_V (= 5/3 \text{ for monatomic})$$

$$e = \frac{|W|}{|Q_H|} = 1 - \frac{|Q_C|}{|Q_H|}$$

$$|Q_H| = |W| + |Q_C|$$

$$\frac{|Q_C|}{|Q_H|} = \frac{T_C}{T_H} \text{ (Carnot engine)}$$

$$\Delta S = Q/T \text{ (Reversible processes)}$$

Waves

$$f = 1/T$$

$$v = f\lambda$$

$$v_{\text{string_wave}} = \sqrt{\frac{\text{Tension}}{m/L}}$$

$$v_{\text{sound_wave}} = \sqrt{\frac{\gamma kT}{m}}$$